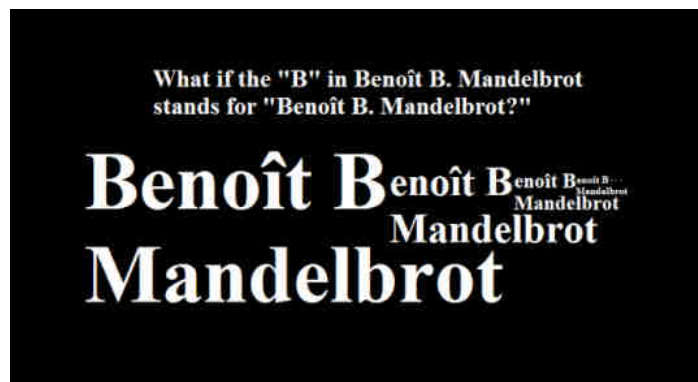
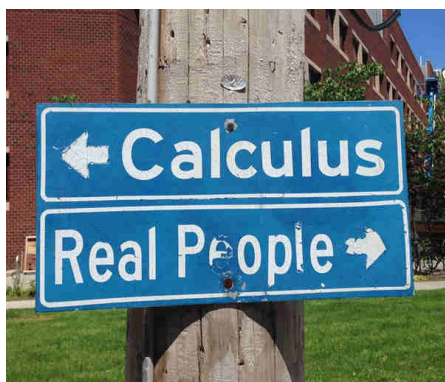
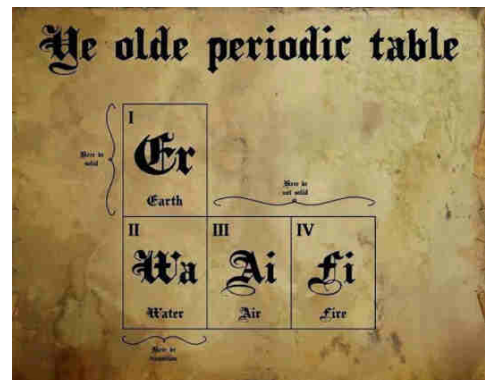
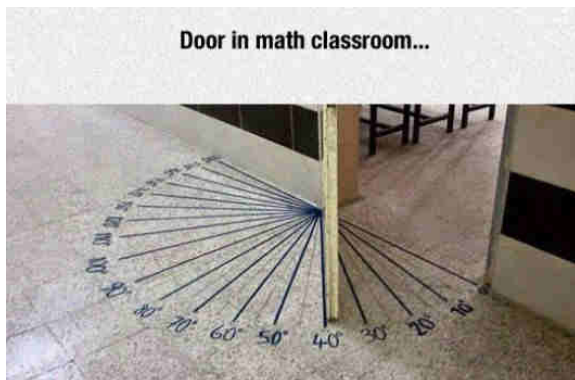
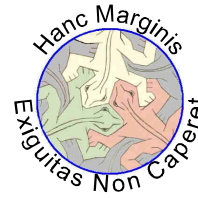




$$x^3 - 6'150x^2 + 12'606'716x - 8'613'517'800 = 0$$





1	S	(1803) Guglielmo Libri Carucci dalla Sommaja (1878) Agner Krarup Erlang (1894) Satyendranath Bose (1912) Boris Gnedenko	RM132 RM168	
2	S	(1822) Rudolf Julius Emmanuel Clausius (1905) Lev Genrichovich Shnirelman (1938) Anatoly Samoilenko	RM240	
1	3	M	(1777) Louis Poinsot (1917) Yuri Alexeievich Mitropolsky	
4	T	(1643) Isaac Newton	RM071	
5	W	(1838) Marie Ennemond Camille Jordan (1871) Federigo Enriques (1871) Gino Fano	RM084	
6	T	(1807) Jozeph Mitza Petzval (1841) Rudolf Sturm		
7	F	(1871) Felix Edouard Justin Émile Borel (1907) Raymond Edward Alan Christopher Paley (1925) Walter Noll		
8	S	(1888) Richard Courant (1924) Paul Moritz Cohn (1942) Stephen William Hawking	RM156	
9	S	(1864) Vladimir Adreievich Steklov (1882) Pavel Aleksandrovitch Florenskij (1915) Mollie Orshansky	RM252	
2	10	M	(1875) Issai Schur (1905) Ruth Moufang	
11	T	(1545) Guidobaldo del Monte (1707) Vincenzo Riccati (1734) Achille Pierre Dionis du Séjour	RM120	
12	W	(1853) Gregorio Ricci-Curbastro (1906) Kurt August Hirsch (1915) Herbert Ellis Robbins	RM156	
13	T	(1864) Wilhelm Karl Werner Otto Fritz Franz Wien (1876) Luther Pfahler Eisenhart (1876) Erhard Schmidt		
14	F	(1901) Alfred Tarski	RM096	
15	S	(1704) Johann Castillon (1717) Matthew Stewart (1850) Sofia Vasilievna Kovalevskaya	RM144	
16	S	(1801) Thomas Klausen		
3	17	M	(1647) Catherina Elisabetha Koopman Hevelius (1847) Nikolay Egorovich Zukowsky (1858) Gabriel Koenigs	RM264
18	T	(1856) Luigi Bianchi (1880) Paul Ehrenfest	RM204	
19	W	(1813) Rudolf Friedrich Alfred Clebsch (1879) Guido Fubini (1908) Aleksandr Gennadievich Kurosh		
20	T	(1775) André Marie Ampère (1895) Gabor Szegő (1904) Renato Caccioppoli	RM072	
21	F	(1846) Pieter Hendrik Schoute (1882) Pavel Aleksandrovitch Florenskij (1915) Yuri Vladimirovich Linnik	RM252	
22	S	(1561) Francis Bacon (1592) Pierre Gassendi (1908) Lev Davidovich Landau	RM228	
23	S	(1840) Ernst Abbe (1862) David Hilbert	RM060	
4	24	M	(1891) Abram Samoilovitch Besicovitch (1902) Oskar Morgenstern (1914) Vladimir Petrovich Potapov	
25	T	(1627) Robert Boyle (1736) Joseph-Louis Lagrange (1843) Karl Hermann Amandus Schwarz	RM048	
26	W	(1799) Benoît Paul Émile Clapeyron (1849) Francesco Flores D'Arcais (1862) Eliakim Hastings Moore		
27	T	(1832) Charles Lutwidge Dodgson	RM108	
28	F	(1611) Johannes Hevelius (1701) Charles Marie de La Condamine (1892) Carlo Emilio Bonferroni	RM264	
29	S	(1817) William Ferrel (1888) Sidney Chapman		
30	S	(1619) Michelangelo Ricci	RM216	
5	31	M	(1715) Giovanni Francesco Fagnano dei Toschi (1841) Samuel Loyd (1896) Sofia Alexandrovna Janowskaja	RM192

Putnam 2007, A1

Find all values of a for which the curves $y = ax^2 + ax + 1/24$ and $x = ay^2 + ay + 1/24$ are tangent to each other.

Why "π" is inferior to "e"

You can't confuse e with a food product.

Why "e" is inferior to "π"

e is less challenging to spell than π .

Why Astronomy is better than sex

If you get tired, wait ten minutes and try it again.

In the mathematics I can report no deficiency, except it be that men do not sufficiently understand this excellent use of the pure mathematics, in that they do remedy and cure many defects in the wit and faculties intellectual. For if the wit be too dull, they sharpen it; if too wandering, they fix it; if too inherent in the sense, they abstract it. So that as tennis is a game of no use in itself, but of great use in respect it maketh a quick eye and a body ready to put itself into all postures, so in the mathematics that use which is collateral and intervenient is no less worthy than that which is principal and intended.

Francis Bacon

Thousands of mystics of all time have knocked with tenfold force on the windows and doors of the palace of science, and if they don't let them in graciously they will enter using force, breaking down precious doors in their path.

Pavel Aleksandrovitch Florenskij

The most distinctive characteristic which differentiates mathematics from the various branches of empirical science, and which accounts for its fame as the queen of the sciences, is no doubt the peculiar certainty and necessity of its results.

Carl G. Hempel

A problem in number theory is as timeless as a true work of art.

David Hilbert

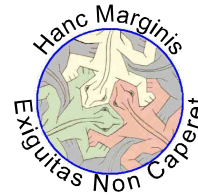
Everyone makes for himself a clear idea of the motion of a point, that is to say, of the motion of a corpuscle which one supposes to be infinitely small, and which one reduces by thought in some way to a mathematical point.

Louis Poinsot

Just as liberal feminists often settle for a minimal program of legal and social equality for women and advocate for the possibility of "choices", so liberal mathematicians (and even some socialists) are often content to work within the hegemonic context of Zermelo-Fraenkel (which, reflecting its nineteenth-century origin, already incorporates the axioms of equality) strengthened only by the axiom of choice. But this framework is wholly insufficient for liberating mathematics, as Paul Cohen proved long ago in 1966.

Alan Sokal

1	T	(1900) John Charles Burkill		
2	W	(1522) Lodovico Ferrari (1893) Cornelius Lanczos (1897) Gertrude Blanch	RM229	
3	T	(1893) Gaston Maurice Julia	RM073	
4	F	(1905) Eric Christopher Zeeman	RM241	
5	S	(1757) Jean Marie Constant Duhamel		
6	S	(1465) Scipione del Ferro (1612) Antoine Arnauld (1695) Nicolaus (II) Bernoulli	RM064 RM093	
6	7	M	(1877) Godfried Harold Hardy (1883) Eric Temple Bell	RM049
8	T	(1700) Daniel Bernoulli (1875) Francis Ysidro Edgeworth (1928) Ennio de Giorgi	RM093 RM133	
9	W	(1775) Farkas Wolfgang Bolyai (1907) Harold Scott Macdonald Coxeter	RM097	
10	T	(1747) Aida Yasuaki (1932) Vivienne Malone-Mayes	RM121	
11	F	(1657) Bernard Le Bovier de Fontenelle (1800) William Henry Fox Talbot (1839) Josiah Willard Gibbs (1915) Richard Wesley Hamming	RM205	
12	S	(1914) Hanna Caemmerer Neumann (1921) Kathleen Rita McNulty Mauchly Antonelli		
13	S	(1805) Johann Peter Gustav Lejeune Dirichlet	RM145	
7	14	M	(1468) Johann Werner (1849) Hermann Hankel (1877) Edmund Georg Hermann Landau (1896) Edward Artur Milne (1932) Maurice Audin	RM253 RM063 RM194
15	T	(1564) Galileo Galilei (1850) Sophie Willock Bryant (1861) Alfred North Whitehead (1946) Douglas Hofstadter	RM085	
16	W	(1822) Francis Galton (1903) Beniamino Segre		
17	T	(1890) Sir Ronald Aylmer Fisher (1891) Adolf Abraham Halevi Fraenkel (1905) Rózsa Péter		
18	F	(1404) Leon Battista Alberti (1919) Clifford Ambrose Truesdell III	RM157	
19	S	(1473) Nicolaus Copernicus	RM181	
20	S	(1844) Ludwig Boltzmann	RM061	
8	21	M	(1591) Girard Desargues (1915) Evgeny Michailovich Lifshitz	
22	T	(1857) Heinrich Rudolf Hertz (1903) Frank Plumpton Ramsey	RM217	
23	W	(1561) Henry Briggs (1583) Jean-Baptiste Morin (1730) Giulio Giuseppe Mozzi del Garbo (1905) Derrick Henry Lehmer (1922) Anneli Cahn Lax (1951) Shigefumi Mori	RM169 RM215	
24	T	(1871) Felix Bernstein		
25	F	(1827) Henry Watson		
26	S	(1786) Dominique Francois Jean Arago	RM193	
27	S	(1881) Luitzen Egbertus Jan Brouwer		
9	28	M	(1735) Alexandre Théophile Vandermonde	RM265
29		(1860) Herman Hollerith	RM109	



Putnam 2007, A2

Find the least possible area of a convex set in the plane that intersects both branches of the hyperbola $xy = 1$ and both branches of the hyperbola $xy = -1$. (A set S in the plane is called *convex* if for any two points in S the line segment connecting them is contained in S .)

Why “ π ” is inferior to “ e ”

You don't need to know Greek to be able to use e .

Why “ e ” is inferior to “ π ”

$e \approx 2.718281828459045$, which can be easily memorized to its billionth place, whereas π needs “skills” to be memorized.

Why Astronomy is better than sex

Nobody cares if you are ugly.

We did have desk calculators at that time, mechanical and driven with electric motors, that could do simple arithmetic. You'd do a multiplication and when the answer appeared, you had to write it down to reenter it into the machine to do the next calculation. We were preparing a firing table for each gun, with maybe 1800 simple trajectories. To hand-compute just one of these trajectories took 30 or 40 hours of sitting at a desk with paper and a calculator. As you can imagine, they were soon running out of young women to do the calculations. Actually, my title working for the ballistics project was “computer”. The idea was that I not only did arithmetic but also made the decision on what to do next. ENIAC made me, one of the first “computers”, obsolete.

Kathleen Rita McNulty Mauchly Antonelli

Nothing proves more clearly that the mind seeks truth, and nothing reflects more glory upon it, than the delight it takes, sometimes in spite of itself, in the driest and thorniest researches of algebra.

Bernard Le Bovier De Fontenelle

Whereas at the outset geometry is reported to have concerned herself with the measurement of muddy land, she now handles celestial as well as terrestrial problems: she has extended her domain to the furthest bounds of space.

W.B. Frankland

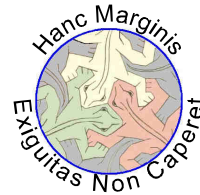
[Statistics are] the only tools by which an opening may be cut through the formidable thicket of difficulties that bars the path of those who pursue the Science of Man.

Francis Galton

Life is an offensive, directed against the repetitious mechanism of the Universe.

Alfred North Whitehead

1	T	(1611) John Pell (1879) Robert Daniel Carmichael		
2	W	(1836) Julius Weingarten		
3	T	(1838) George William Hill (1845) Georg Cantor (1916) Paul Richard Halmos	RM062	
4	F	(1822) Jules Antoine Lissajous		
5	S	(1512) Gerardus Mercator (1759) Benjamin Gompertz (1817) Angelo Genocchi (1885) Pauline Sperry (1915) Laurent Schwartz (1931) Vera Pless	RM230 RM194	
6	S	(1866) Ettore Bortolotti		
10	7	M	(1792) William Herschel (1824) Delfino Codazzi (1922) Olga Alexandrovna Ladyzhenskaya	RM146
8	T	(1851) George Chrystal		
9	W	(1818) Ferdinand Joachimsthal (1900) Howard Hathaway Aiken		
10	T	(1864) William Fogg Osgood (1872) Mary Ann Elizabeth Stephansen		
11	F	(1811) Urbain Jean Joseph Le Verrier (1853) Salvatore Pincherle (1870) Louis Bachelier	RM158	
12	S	(1685) George Berkeley (1824) Gustav Robert Kirchhoff (1859) Ernesto Cesaro		
13	S	(1861) Jules Joseph Drach (1957) Rudy D'Alembert		
11	14	M	(1864) Jozef Kurschak (1879) Albert Einstein (1882) Wacław Sierpiński (1904) Lyudmila Vsevolodovna Keldysh	RM074 RM271 RM266
15	T	(1860) Walter Frank Raphael Weldon (1868) Grace Chisolm Young		
16	W	(1750) Caroline Herschel (1789) Georg Simon Ohm (1846) Magnus Gosta Mittag-Leffler	RM146	
17	T	(1876) Ernest Benjamin Esclangon (1897) Charles Fox (1915) Wolfgang (Vincent) Döblin (Doblin)	RM254	
18	F	(1640) Philippe de La Hire (1690) Christian Goldbach (1796) Jacob Steiner (1870) Agnes Sime Baxter	RM122	
19	S	(1862) Adolf Kneser (1910) Jacob Wolfowitz		
20	S	(1840) Franz Mertens (1884) Philip Franck (1938) Sergei Petrovich Novikov		
12	21	M	(1768) Jean Baptiste Joseph Fourier (1884) George David Birkhoff	RM242
22	T	(1394) Ulugh Beg (1891) Lorna Mary Swain (1917) Irving Kaplansky (1944) Margaret Hilary Ashworth Millington	RM206	
23	W	(1749) Pierre-Simon de Laplace (1754) Georg Freiherr von Vega (1882) Emmy Amalie Noether (1897) John Lighton Synge	RM050	
24	T	(1809) Joseph Liouville (1948) Sun-Yung (Alice) Chang (1966) Gigliola Staffilani	RM142	
25	F	(1538) Christopher Clausius		
26	S	(1848) Konstantin Andreev (1913) Paul Erdős	RM110	
27	S	(1857) Karl Pearson		
13	28	M	(1928) Alexander Grothendieck	RM086
29	T	(1825) Francesco Faà Di Bruno (1873) Tullio Levi-Civita (1896) Wilhelm Ackermann	RM170 RM098	
30	W	(1892) Stefan Banach (1921) Alfréd Rényi	RM134	
31	T	(1596) René Descartes	RM218	



March

Putnam 2007, A3

Let k be a positive integer. Suppose that the integers $1, 2, 3, \dots, 3k + 1$ are written down in random order. What is the probability that at no time during this process, the sum of the integers that have been written up to that time is a positive integer divisible by 3? Your answer should be in closed form, but may include factorials.

Why " π " is inferior to " e "

e stands for Euler's Number, π doesn't stand for squat.

Why " e " is inferior to " π "

To read π , you don't have to know that Euler's name is really pronounced Oiler.

Why Astronomy is better than sex

Forty years from now, you can still participate regularly.

There should be a general science that explains everything that can be known about order and measure, considered independently of each application to a particular subject [...] and indeed this science has a proper name, consecrated by a long use, which is mathematics.

René Descartes

The most beautiful thing we can experience is the mysterious. It is the source of all true art and science.

Albert Einstein

[About Fourier] It was, no doubt, partially because of his very disregard for rigor that he was able to take conceptual steps which were inherently impossible to men of more critical genius.

Rudolph E. Langer

It is India that gave us the ingenious method of expressing all numbers by means of ten symbols, each symbol receiving a value of position as well as an absolute value; a profound and important idea which appears so simple to us now that we ignore its true merit. But its very simplicity and the great ease which it has lent to computations put our arithmetic in the first rank of useful inventions; and we shall appreciate the grandeur of the achievement the more when we remember that it escaped the genius of Archimedes and Apollonius, two of the greatest men produced by antiquity.

Pierre-Simon De Laplace

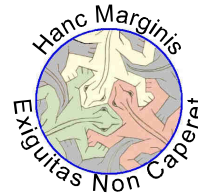
The mathematician, carried on by his river of symbols, dealing with what appears to be purely formal truth, can nevertheless achieve results of endless importance for our description of the physical universe.

Karl Pearson

[told by David Harbater] Starting with 75 students, the class quickly dwindled to 20 by the end of the second semester. Of these, only ten really knew what they were doing. Of those ten, eight would become math professors and one physics professors. The tenth was Richard Stallman.

Richard Matthew Stallman

1	F	(1640) Georg Mohr (1776) Marie-Sophie Germain (1895) Alexander Craig Aitken	RM219	
2	S	(1878) Edward Kasner (1934) Paul Joseph Cohen (1984) Alessio Figalli	RM243	
3	S	(1835) John Howard Van Amringe (1892) Hans Rademacher (1900) Albert Edward Ingham (1971) Alice Riddle		
14	4	M	(1809) Benjamin Peirce (1842) François Édouard Anatole Lucas (1949) Shing-Tung Yau	RM123
	5	T	(1588) Thomas Hobbes (1607) Honoré Fabri (1622) Vincenzo Viviani (1869) Sergei Alexeievich Chaplygin	
	6	W	(1801) William Hallowes Miller	
	7	T	(1768) François-Joseph Français	
	8	F	(1903) Marshall Harvey Stone	
	9	S	(1791) George Peacock (1816) Charles Eugene Delaunay (1894) Cypra Cecilia Krieger Dunaij (1919) John Presper Heckert	
	10	S	(1857) Henry Ernest Dudeney	RM183
15	11	M	(1953) Andrew John Wiles	RM207
	12	T	(1794) Germinal Pierre Dandelin (1852) Carl Louis Ferdinand von Lindemann (1903) Jan Tinbergen	RM267
	13	W	(1728) Paolo Frisi (1813) Duncan Farquharson Gregory (1869) Ada Isabel Maddison (1879) Francesco Severi (1909) Stanislaw Marcin Ulam	RM171
	14	T	(1629) Christiaan Huygens	RM135
	15	F	(1452) Leonardo da Vinci (1548) Pietro Antonio Cataldi (1707) Leonhard Euler (1809) Herman Gunther Grassmann	RM051
	16	S	(1682) John Hadley (1823) Ferdinand Gotthold Max Eisenstein	
	17	S	(1798) Étienne Bobillier (1853) Arthur Moritz Schonflies (1863) Augustus Edward Hough Love	
16	18	M	(1791) Ottaviano Fabrizio Mossotti (1907) Lars Valerian Ahlfors (1918) Hsien Chung Wang (1949) Charles Louis Fefferman	RM150
	19	T	(1880) Evgeny Evgenievich Slutsky (1883) Richard von Mises (1901) Kiyoshi Oka (1905) Charles Ehresmann	
	20	W	(1839) Francesco Siacchi	
	21	T	(1652) Michel Rolle (1774) Jean Baptiste Biot (1875) Teiji Takagi	RM231
	22	F	(1811) Otto Ludwig Hesse (1887) Harald August Bohr (1935) Bhama Srinivasan (1939) Sir Michael Francis Atiyah	RM063
	23	S	(1858) Max Karl Ernst Ludwig Planck (1910) Sheila Scott Macintyre	
	24	S	(1863) Giovanni Vailati (1899) Oscar Zariski	RM099
17	25	M	(1849) Felix Christian Klein (1900) Wolfgang Pauli (1903) Andrei Nicolayevich Kolmogorov	RM255 RM159
	26	T	(1889) Ludwig Josef Johan Wittgenstein	
	27	W	(1755) Marc-Antoine Parseval des Chenes (1932) Gian-Carlo Rota	RM195
	28	T	(1906) Kurt Gödel	RM087
	29	F	(1854) Jules Henri Poincaré	RM075
	30	S	(1777) Johann Carl Friedrich Gauss (1916) Claude Elwood Shannon	RM147 RM111



Putnam 2007, A4

A *repunit* is a positive integer whose digits in base 10 are all ones. Find all polynomials f with real coefficients such that if n is a repunit, then so is $f(n)$.

Why “ π ” is inferior to “ e ”

e is easier to spell than π .

Why “ e ” is inferior to “ π ”

The character for e is so cheap that it can be found on a keyboard. But π is special (it’s under “special symbols” in word processor programs.).

Why Astronomy is better than sex

Doesn’t matter if kids hear you moaning, oohing and aahing.

It is the most self-evident truth, immediately evident to unsophisticated observation, that mathematics is a human invention.

Percy Williams Bridgman

Finally, two days ago, I succeeded – not on account of my hard efforts, but by the grace of the Lord. Like a sudden flash of lightning, the riddle was solved. I am unable to say what was the conducting thread that connected what I previously knew with what made my success possible.

Johann Carl Friedrich Gauss

... the science of calculus is even indispensable up to the extraction of square and cubic roots; algebra up to second degree equations and the use of logarithms often has value in the usual cases; but all that beyond that is mere lust. A delightful lust, nothing to say: but which must not indulge anyone who has to execute a profession for his subsistence.

Thomas Jefferson

What is it indeed that gives us the feeling of elegance in a solution, in a demonstration? It is the harmony of the diverse parts, their symmetry, their happy balance; in a word it is all that introduces order, all that gives unity, that permits us to see clearly and to comprehend at once both the ensemble and the details.

Jules Henri Poincaré

Though this be madness, yet there is method in’t.

William Shakespeare

For all their wealth of content, for all the sum of history and social institution invested in them, music, mathematics, and chess are resplendently useless (applied mathematics is a higher plumbing, a kind of music for the police band). They are metaphysically trivial, irresponsible. They refuse to relate outward, to take reality for arbiter. This is the source of their witchery.

G. Steiner

After watching a thunderstorm, when asked “how many raindrops did you see?” the most suitable answer is “many”: not that the precise number does not exist, but it cannot be known.

Ludwig Josef Johan Wittgenstein

1	S	(1825) Johann Jacob Balmer (1908) Morris Kline (1977) Maryam Mirzakhani	RM122 RM189	
18	2	M	(1860) D'Arcy Wentworth Thompson (1905) Kazimierz Zarankiewicz	RM138
	3	T	(1842) Otto Stolz (1860) Vito Volterra (1892) George Paget Thomson	RM136 RM161
	4	W	(1845) William Kingdon Clifford	
	5	T	(1833) Lazarus Emmanuel Fuchs (1883) Anna Johnson Pell Wheeler (1889) René Eugène Gateaux (1897) Francesco Giacomo Tricomi (1923) Cathleen Synge Morawetz	RM196 RM256
	6	F	(1872) Willem de Sitter (1906) André Weil	RM088
	7	S	(1854) Giuseppe Veronese (1881) Ebenezer Cunningham (1896) Pavel Sergievich Alexandrov (1926) Alexis Claude Clairaut	RM220
	8	S	(1859) Johan Ludwig William Valdemar Jensen (1905) Winifred Lydia Caunden Sargent	
19	9	M	(1746) Gaspard Monge (1876) Gilbert Ames Bliss (1965) Karen Ellen Smith	RM208
	10	T	(1788) Augustin Jean Fresnel (1847) William Karl Joseph Killing (1904) Edward James Mcshane (1958) Piotr Rezierovich Silverbrahms	
	11	W	(1902) Edna Ernestine Kramer Lassar (1918) Richard Phillips Feynman	RM076
	12	T	(1820) Florence Nightingale (1845) Pierre René Jean Baptiste Henry Brocard (1902) Frank Yates	RM104
	13	F	(1750) Lorenzo Mascheroni (1899) Pelageia Yakovlevna Polubarinova Kochina	
	14	S	(1832) Rudolf Otto Sigismund Lipschitz (1863) John Charles Fields	RM100
	15	S	(1939) Brian Hartley (1964) Sijue Wu	
20	16	M	(1718) Maria Gaetana Agnesi (1821) Pafnuti Lvovi Chebyshev (1911) John (Jack) Todd	RM112 RM139
	17	T	(1940) Alan Kay	
	18	W	(1850) Oliver Heaviside (1892) Bertrand Arthur William Russell	RM160 RM052
	19	T	(1865) Flora Philip (1919) Georgii Dimitrievich Suvorov	
	20	F	(1861) Henry Seely White	
	21	S	(1471) Albrecht Dürer (1792) Gustave Gaspard de Coriolis	RM124
	22	S	(1865) Alfred Cardew Dixon	
21	23	M	(1914) Lipa Bers	RM148
	24	T	(1544) William Gilbert	
	25	W	(1838) Karl Mikailovich Peterson (1979) Elena Tosato	RM268
	26	T	(1667) Abraham de Moivre (1896) Yuri Dimitrievich Sokolov	
	27	F	(1862) John Edward Campbell	
	28	S	(1676) Jacopo Francesco Riccati (1710) Johann (II) Bernoulli	RM232 RM093
	29	S	(1882) Harry Bateman	
22	30	M	(1814) Eugene Charles Catalan	RM184
	31	T	(1926) John Kemeny	



Putnam 2007, A5

Suppose that a finite group has exactly n elements of order p , where p is a prime. Prove that either $n = 0$ or p divides $n + 1$.

Why “ π ” is inferior to “ e ”

$\pi \approx 3.14$ while $e \approx 2.718281828459045$.

Why “ e ” is inferior to “ π ”

π is much shorter and easier to say than “Euler’s Number”.

Why Astronomy is better than sex

You can do it all night.

The mathematician begins with a few propositions, the proof of which is so obvious that they are said to be obvious, and the rest of his work consists of ingenious deductions from them. Language teaching, as practiced in general, is of the same general nature: authority and tradition provide the data, and mental operations are deductive.

Thomas Henry Huxley

Projective geometry: a limitless domain of countless fields where real and imaginary, finite and infinite, enter into full equality, where the spirit delights in the artistic balance and symmetrical reciprocity of a sort of conceptual and logical counterpoint – an enchanted realm where thought splits and flows everywhere in parallel flows.

Cassius Jackson Keyser

Reine Mathematik ist Religion – Pure mathematics is religion.

Novalis

The method of “postulating” what we want has many advantages; they are the same as the advantages of theft over honest toil.

Bertrand Arthur William Russell

Did you know? The square built on the hypotenuse is double the one on the catheti but the quality is poor and after a year you throw it away! That’s it! It happened to my sister! Trust me!

Vulvia

Nobody since Newton has been able to use geometrical methods to the same extent for the like purposes; and as we read the Principia we feel as when we are in an ancient armoury where the weapons are of gigantic size; and as we look at them we marvel what manner of man he was who could use as a weapon what we can scarcely lift as a burden.

William Whewell



1	W	(1796) Sadi Leonard Nicolas Carnot (1851) Edward Bailey Elliott (1899) Edward Charles Titchmarsh	
2	T	(1895) Tibor Radó	
3	F	(1659) David Gregory (1954) Susan Landau	
4	S	(1809) John Henry Pratt (1966) Svetlana Yakovlevna Jitomirskaya	RM197
5	S	(1814) Pierre Laurent Wantzel (1819) John Couch Adams (1883) John Maynard Keynes	RM065 RM269
23	6	M	(1436) Johann Müller Regiomontanus RM185 (1857) Aleksandr Michailovitch Lyapunov RM077 (1906) Max August Zorn
	7	T	(1863) Edward Burr Van Vleck
	8	W	(1625) Giovanni Domenico Cassini RM245 (1858) Charlotte Angas Scott (1860) Alicia Boole Stott (1896) Eleanor Pairman RM209 (1923) Gloria Olive (1924) Samuel Karlin
	9	T	(1885) John Edensor Littlewood RM049
	10	F	(940) Mohammad Abu'L Wafa Al-Buzjani RM257 (1887) Vladimir Ivanovich Smirnov RM101
	11	S	(1881) Hilda Phoebe Hudson (1937) David Bryant Mumford
	12	S	(1888) Zygmunt Janyszewski (1937) Vladimir Igorevich Arnold RM221
24	13	M	(1831) James Clerk Maxwell RM113 (1872) Jessie Chrystal Macmillan (1876) William Sealey Gosset (Student) (1928) John Forbes Nash RM149
	14	T	(1736) Charles Augustin de Coulomb (1856) Andrei Andreyevich Markov RM125 (1903) Alonzo Church RM233
	15	W	(1640) Bernard Lamy (1894) Nikolai Gregorievich Chebotaryov
	16	T	(1915) John Wilder Tukey
	17	F	(1898) Maurits Cornelius Escher RM097
	18	S	(1858) Andrew Russell Forsyth (1884) Charles Ernest Weatherburn (1884) Frieda Nugel (1913) Paul Teichmüller RM148 (1915) Alice Turner Schafer
	19	S	(1623) Blaise Pascal RM053 (1902) Wallace John Eckert
25	20	M	(1873) Alfred Loewy (1917) Helena Rasiowa
	21	T	(1781) Simeon Denis Poisson (1828) Giuseppe Bruno (1870) Maria Skłodowska Curie RM182
	22	W	(1822) Mario Pieri (1864) Hermann Minkowsky (1910) Konrad Zuse (1932) Mary Wynne Warner
	23	T	(1912) Alan Mathison Turing RM089
	24	F	(1880) Oswald Veblen
	25	S	(1908) William Van Orman Quine
	26	S	(1824) William Thomson, Lord Kelvin RM161 (1918) Yudell Leo Luke
26	27	M	(1806) Augustus de Morgan
	28	T	(1875) Henri Léon Lebesgue RM173
	29	W	(1888) Aleksandr Aleksandrovich Friedmann RM101 (1979) Artur Avila Cordeiro de Melo RM189
	30	T	(1791) Felix Savart (1958) Abigail Thompson

Putnam 2007, A6

A triangulation T of a polygon P is a finite collection of triangles whose union is P , and such that the intersection of any two triangles is either empty, or a shared vertex, or a shared side. Moreover, each side is a side of exactly one triangle in T . Say that T is *admissible* if every internal vertex is shared by 6 or more triangles. Prove that there is an integer M_n , depending only on n , such that any admissible triangulation of a polygon P with n sides has at most M_n triangles.

Why “ π ” is inferior to “ e ”

The character for e can be found on a keyboard, but π sure can't.

Why “ e ” is inferior to “ π ”

e is named after a person, but π stands for itself.

Why Astronomy is better than sex

Less guilt the next morning.

Revolutions never occur in mathematics.

Michael Crowe

The nation of Italy, as we know it today, was born in the 1860s following the Risorgimento, a movement of national awareness that flourished around the middle of the nineteenth century. Thus relieved of the distractions of having their own nation, the Italians resumed their great tradition, filling the end of the 19th century with some important scholars: Enrico Betti, Francesco Brioschi, Luigi Cremona, Eugenio Beltrami.

John Derbyshire

Dead scientists tend to become lunar and planetary features, dead mathematicians e-mail servers.

Robert & Ellen Kaplan

A linguist would be shocked to learn that if a set is not closed this does not mean that it is open, or again that “ E is dense in E ” does not mean the same thing as “ E is dense in itself”.

John Edensor Littlewood

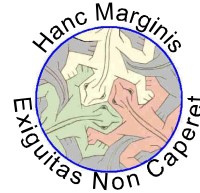
There are two types of mind... the mathematical, and what might be called the intuitive. The former arrives at its views slowly, but they are firm and rigid; the latter is endowed with greater flexibility and applies itself simultaneously to the diverse lovable parts of that which it loves.

Blaise Pascal

Wherever there are numbers there is beauty and we are in the immediate vicinity of art.

Andreas Speiser

1	F	(1643) Gottfried Wilhelm von Leibniz (1788) Jean-Victor Poncelet (1906) Jean Alexandre Eugène Dieudonné	RM054 RM246
2	S	(1820) William John Rankine (1852) William Burnside (1925) Olga Arsen'evna Oleinik	
3	S	(1807) Ernest Jean Philippe Fauque de Jonquières (1897) Jesse Douglas	RM162
27	4	M	(1906) Daniel Edwin Rutherford (1917) Michail Samoilovich Livsic
5	T	(1936) James Mirrlees	
6	W	(1849) Alfred Bray Kempe	
7	T	(1816) Johann Rudolf Wolf (1906) William Feller (1922) Vladimir Aleksandrovich Marchenko	
8	F	(1760) Christian Kramp (1904) Henri Paul Cartan	RM126
9	S	(1845) George Howard Darwin (1931) Valentina Mikhailovna Borok	RM138 RM197
10	S	(1856) Nikola Tesla (1862) Roger Cotes (1868) Oliver Dimon Kellogg	RM174
28	11	M	(1857) Sir Joseph Larmor (1888) Jacob David Tamarkin (1890) Giacomo Albanese
12	T	(1875) Ernest Sigismund Fischer (1895) Richard Buckminster Fuller (1935) Nicolas Bourbaki	RM066 RM126
13	W	(1527) John Dee (1741) Karl Friedrich Hindenburg	RM234
14	T	(1671) Jacques D'Allonville (1793) George Green	RM078
15	F	(1865) Wilhelm Wirtinger (1898) Mary Taylor Slow (1906) Adolph Andrej Pavlovich Yushkevich	
16	S	(1678) Jakob Hermann (1903) Irmgard Flugge-Lotz	
17	S	(1831) Victor Mayer Amédeé Mannheim (1837) Wilhelm Lexis (1944) Krystyna Maria Trybulec Kuperberg	
29	18	M	(1013) Hermann von Reichenau (1635) Robert Hooke (1853) Hendrik Antoon Lorentz
19	T	(1768) Francois Joseph Servois	RM114 RM161
20	W	(1876) Otto Blumenthal (1947) Gerd Binnig	RM258 RM222
21	T	(1620) Jean Picard (1848) Emil Weyr (1849) Robert Simpson Woodward (1861) Herbert Ellsworth Slaught	
22	F	(1784) Friedrich Wilhelm Bessel	RM198
23	S	(1775) Étienne-Louis Malus (1854) Ivan Slezyunsky	
24	S	(1851) Friedrich Hermann Schottky (1871) Paul Epstein (1923) Christine Mary Hamill	
30	25	M	(1808) Johann Benedict Listing
26	T	(1903) Kurt Mahler	
27	W	(1667) Johann Bernoulli (1801) George Biddel Airy (1848) Lorand Baron von Eötvös (1867) Derrick Norman Lehmer (1871) Ernst Friedrich Ferdinand Zermelo	RM093 RM210 RM215 RM090
28	T	(1954) Gerd Faltings	RM222
29	F	(1898) Isidor Isaac Rabi	
30	S	(1889) Vladimir Kosma Zworkyn	
31	S	(1704) Gabriel Cramer (1712) Johann Samuel Koenig (1926) Hilary Putnam	RM186



Putnam 2007, B1

Let f be a polynomial with positive integer coefficients. Prove that if n is a positive integer, then $f(n)$ divides $f(f(n) + 1)$ if and only if $n = 1$. [Editor's note: one must assume f is nonconstant.]

Why "π" is inferior to "e"

Everybody fights for their piece of the pie.

Why "e" is inferior to "π"

People mistakenly confuse Euler's Number (e) with Euler's Constant (γ). There is no confusion with the one and only π .

Why Astronomy is better than sex

You can experience multiple objects in a single session.

Mathematical theories constitute fictional universes, which are not fundamentally dissimilar from those, equally complex and articulated, of the great novels of the twentieth century, such as the Search for lost time or Ulysses.

Claudio Bartocci

Doing physics is much more enjoyable than just learning it. Maybe 'doing it' is the right way of learning, at least as far as I am concerned.

Gerd Binnig

There is nothing in a caterpillar that tells you it's going to be a butterfly.

Richard Buckminster Fuller

We have not begun to understand the relationship between combinatorics and conceptual mathematics.

Jean Alexandre Eugène Dieudonné

For mere human interest, you can't beat TV quizzes to investigate decisional math.

Rob Eastaway E Jeremy Wyndham

It is commonly believed that anyone who tabulates numbers is a statistician. This is like believing that anyone who owns a scalpel is a surgeon.

Robert Hooke

Axioms can be compared to the rules of a game, the value of which cannot be questioned. If you want to change these rules, you must necessarily play another game.

Mario Livio

If your new theorem can be stated with great simplicity, then there will exist a pathological exception.

Adrian Mathesis

All that was great in the past was ridiculed, condemned, combated, suppressed – only to emerge all the more powerfully, all the more triumphantly from the struggle.

Nikola Tesla



31	1	M	(1861) Ivar Otto Bendixson (1881) Otto Toeplitz (1955) Bernadette Perrin-Riou		
	2	T	(1856) Ferdinand Rudio (1902) Mina Spiegel Rees		
	3	W	(1914) Mark Kac	RM115	
	4	T	(1805) Sir William Rowan Hamilton (1838) John Venn	RM079	
	5	F	(1802) Niels Henrik Abel (1941) Alexander Keewatin Dewdney	RM055	
	6	S	(1638) Nicolas Malebranche (1741) John Wilson		
	7	S	(1868) Ladislaus Josephowitsch Bortkiewitz		
32	8	M	(1902) Paul Adrien Maurice Dirac (1931) Sir Roger Penrose (1974) Manjul Bhargava	RM103 RM189	
	9	T	(1537) Francesco Barozzi (Franciscus Barocius) (1940) Linda Goldway Keen	RM223	
	10	W	(1602) Gilles Personne de Roberval (1901) Franco Dino Rasetti (1926) Carol Ruth Karp	RM235	
	11	T	(1730) Charles Bossut (1842) Enrico D'Ovidio	RM259	
	12	F	(1882) Jules Antoine Richard (1887) Erwin Rudolf Josef Alexander Schrödinger	RM103	
	13	S	(1625) Erasmus Bartholin (1819) George Gabriel Stokes (1861) Cesare Burali-Forti	RM187	
	14	S	(1530) Giovanni Battista Benedetti (1842) Jean Gaston Darboux (1865) Guido Castelnuovo (1866) Charles Gustave Nicolas de La Vallée-Poussin		
	33	15	M	(1863) Aleksei Nikolaevich Krylov (1892) Louis Pierre Victor Duc de Broglie (1901) Piotr Sergeevich Novikov	RM175
		16	T	(1773) Louis-Benjamin Francoeur (1821) Arthur Cayley	
		17	W	(1601) Pierre de Fermat	RM091
		18	T	(1685) Brook Taylor	
		19	F	(1646) John Flamsteed (1739) Georg Simon Klügel	
		20	S	(1710) Thomas Simpson (1863) Corrado Segre	RM247
		21	S	(1789) Augustin-Louis Cauchy	RM127
34		22	M	(1647) Denis Papin	
		23	T	(1683) Giovanni Poleni (1829) Moritz Benedikt Cantor (1842) Osborne Reynolds	
	24	W	(1561) Bartholomeo Pitiscus (1942) Karen Keskulla Uhlenbeck	RM163	
	25	T	(1561) Philip Van Lansberge (1844) Thomas Muir	RM199	
	26	F	(1728) Johann Heinrich Lambert (1875) Giuseppe Vitali (1965) Marcus Peter Francis du Sautoy		
	27	S	(1858) Giuseppe Peano	RM067	
	28	S	(1796) Irénée Jules Bienaymé (1862) Roberto Marcolongo	RM187	
	35	29	M	(1904) Leonard Roth	
		30	T	(1703) Giovanni Ludovico Calandrini (1856) Carle David Tolmé Runge (1906) Olga Taussky-Todd	RM186 RM139
		31	W	(1821) Hermann Ludwig Ferdinand von Helmholtz (1885) Herbert Westren Turnbull	RM211

Putnam 2007, B2

Suppose that $f: [0, 1] \rightarrow \mathbb{R}$ has a continuous derivative and that $\int_0^1 f(x)dx = 0$. Prove that for every $\alpha \in (0, 1)$,

$$\left| \int_0^\alpha f(x)dx \right| \leq \frac{1}{8} \max_{0 \leq x \leq 1} |f'(x)|.$$

Why “ π ” is inferior to “ e ”

$\ln(\pi^2)$ is a really nasty number, but $\ln(e^2)=1$.

Why “ e ” is inferior to “ π ”

You understand what e is even though you start learning it late when you're in pre-calculus. But with π , even after five or six years, it's still hard to know what it really is.

Why Astronomy is better than sex

The person you're with doesn't fantasize you're someone else.

When you discover things about numbers, it's very beautiful, when mathematicians are thinking about their problems, we're not thinking about their various applications, but rather are pursuing beauty. That's how pure mathematicians think.

Manjul Bhargava

I crave the liberty to conceal my name, not to suppress it. I have composed the letters of it written in Latin in this sentence — In Mathesi a sole fundes. [Anagram from Latinized name, Johannes Flamsteedius].

John Flamsteed

Perhaps it was precisely such a cumbersome mathematical notation [Roman numerals] that did not make Romans excellent mathematicians. It could be argued that they were nevertheless excellent engineers. “Exactly!”, Many mathematicians would reply.

Furio Honsell

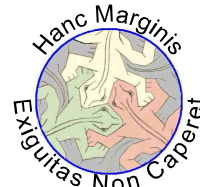
Mathematical economics is old enough to be respectable, but not all economists respect it. It has powerful supporters and impressive testimonials, yet many capable economists deny that mathematics, except as a shorthand or expository device, can be applied to economic reasoning. There have even been rumors that mathematics is used in economics (and in other social sciences) either for the deliberate purpose of mystification or to confer dignity upon common places as French was once used in diplomatic communications.

James R. Newman

I can not help thinking that, in the case of mathematics, the arguments to believe in a possible ethereal, eternal existence, at least for the deeper mathematical concepts, are much stronger than those that lead to infer a discovery of the other cases of human activity.

Sir Roger Penrose

1	T	(1647) Giovanni Ceva (1659) Joseph Saurin (1835) William Stanley Jevons	RM203	
2	F	(1878) Maurice René Frechet (1923) René Thom	RM080	
3	S	(1814) James Joseph Sylvester (1884) Solomon Lefschetz (1908) Lev Semenovich Pontryagin	RM104	
4	S	(1809) Luigi Federico Menabrea	RM150	
36	5	M	(1667) Giovanni Girolamo Saccheri (1725) Jean-Étienne Montucla	RM128
6	T	(1859) Boris Jakovlevich Bukreev (1863) Dimitri Aleksandrovich Grave		
7	W	(1707) George Louis Leclerc Comte de Buffon (1948) Cheryl Elisabeth Praeger (1955) Efim Zelmanov		
8	T	(1584) Gregorius Saint-Vincent (1588) Marin Mersenne	RM092	
9	F	(1860) Frank Morley (1914) Marjorie Lee Browne		
10	S	(1839) Charles Sanders Peirce	RM123	
11	S	(1623) Stefano degli Angeli (1798) Franz Ernst Neumann (1877) Sir James Hopwood Jeans	RM224	
37	12	M	(1891) Antoine André Louis Reynaud (1894) Dorothy Maud Wrinch (1900) Haskell Brooks Curry	RM260 RM212
13	T	(1873) Constantin Carathéodory (1885) Wilhelm Johann Eugen Blaschke		
14	W	(1858) Henry Burchard Fine (1891) Ivan Matveevich Vinogradov		
15	T	(973) Abu Arrayhan Muhammad Ibn Ahmad Al'Biruni (1886) Paul Pierre Levy	RM164	
16	F	(1494) Francisco Maurolico (1736) Johann Nikolaus Tetens		
17	S	(1743) Marie Jean Antoine Nicolas de Caritat de Condorcet (1826) Georg Friedrich Bernhard Riemann	RM176 RM068	
18	S	(1752) Adrien-Marie Legendre	RM140	
38	19	M	(1749) Jean-Baptiste Delambre	
20	T	(1842) Alexander Wilhelm von Brill (1861) Frank Nelson Cole		
21	W	(1899) Juliusz Pawel Schauder (1917) Phyllis Nicolson		
22	T	(1765) Paolo Ruffini (1769) Louis Puissant (1803) Jaques Charles Francois Sturm	RM116	
23	F	(1768) William Wallace (1900) David Van Dantzig		
24	S	(1501) Girolamo Cardano (1625) Johan de Witt (1801) Michail Vasilevich Ostrogradski (1862) Winifred Edgerton Merrill (1945) Ian Nicholas Stewart	RM064 RM188 RM056 RM236	
25	S	(1819) George Salmon (1888) Stefan Mazurkiewicz		
39	26	M	(1688) Willem Jakob 's Gravesande (1854) Percy Alexander Macmahon (1891) Hans Reichenbach	
27	T	(1855) Paul Émile Appell (1876) Earle Raymond Hedrick (1919) James Hardy Wilkinson		
28	W	(1698) Pierre Louis Moreau de Maupertuis (1761) Ferdinand François Desiré Budan de Boislaurent (1873) Julian Lowell Coolidge	RM152	
29	T	(1540) François Viète (1561) Adriaan Van Roomen (1812) Adolph Gopel	RM200 RM200	
30	F	(1775) Robert Adrain (1829) Joseph Wolstenholme (1883) Ernst Hellinger (1891) Otto Yulyevich Schmidt	RM248	



Putnam 2007, B3

Let $x_0 = 1$ and for $n \geq 0$, let $x_{n+1} = 3x_n + \lfloor x_n \sqrt{5} \rfloor$. In particular, $x_1 = 5$, $x_2 = 26$, $x_3 = 136$, $x_4 = 712$. Find a closed-form expression for x_{2007} . ($\lfloor a \rfloor$ means the largest integer $\leq a$.)

Why “ π ” is inferior to “ e ”

e is used in calculus while π is used in baby geometry.

Why “ e ” is inferior to “ π ”

e has an easy limit definition and infinite series. The limit definition of π and the infinite series are much harder.

Why Astronomy is better than sex

There is no shame when purchasing the equipment.

“It seems to me that you beg the question,” Haydock said, “and I see one of those terrible exercises in probability looming where six men wear white hats and six other black hats, and you must mathematically derive the probability that the hats are mixed and in what proportion.”

“If you start thinking about things like that, you go crazy. I assure you!”

Agatha Christie

Here is where the human mind is: on the one hand, subject to the laws of physics and the biological imperatives of evolution; on the other, as a small wheel in the gears of the enormous machine of human society. Our appreciation for music arose from the interplay of these two influences. That’s why music has clear elements of mathematical patterns, but is generally best when it throws away the pattern book and draws on elements of human culture and emotions that are – at least for now – beyond scientific understanding.

Jack Cohen, Terry Pratchett, Ian Stewart

Mathematics can be considered as that which unites and interposes Man and Nature, the external and internal world, thought and perception.

Friedrich Wilhelm August Fröbel

The human activities that persist in keeping a dream alive, despite the overwhelming evidence to the contrary, can be counted on the fingers of one hand: religion, theoretical physics, being a fan of the Belgian football team, and ... mathematics.

Lieven Le Bruyn

(after Edna St. Vincent Millay)

...Euclid alone

Has looked on Beauty bare.

He turned away at once;

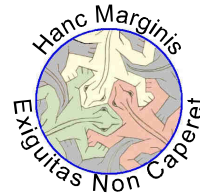
Far too polite to stare.

Adrian Riskin

Computers are smart machines, but they are useless without some good mathematics.

Ian Nicholas Stewart

1	S	(1671) Luigi Guido Grandi (1898) Bela Kerekjarto' (1912) Kathleen Timpson Ollerenshaw	RM177
2	S	(1825) John James Walker (1908) Arthur Erdélyi	
40	3	M	(1944) Pierre René Deligne
4	T	(1759) Louis Francois Antoine Arbogast (1797) Jerome Savary	
5	W	(1732) Nevil Maskelyne (1781) Bernhard Placidus Johann Nepomuk Bolzano (1861) Thomas Little Heath	RM117
6	T	(1552) Matteo Ricci (1831) Julius Wilhelm Richard Dedekind (1908) Sergei Lvovich Sobolev	RM141 RM081
7	F	(1885) Niels Bohr	RM063
8	S	(1908) Hans Arnold Heilbronn	
9	S	(1581) Claude Gaspard Bachet de Meziriac (1704) Johann Andrea von Segner (1873) Karl Schwarzschild (1949) Fan Rong K Chung Graham	RM201 RM153 RM110
41	10	M	(1731) Henry Cavendish (1861) Heinrich Friedrich Karl Ludwig Burkhardt
11	T	(1675) Samuel Clarke (1777) Barnabè Brisson (1881) Lewis Fry Richardson (1885) Alfred Haar (1910) Cahit Arf	RM273 RM261
12	W	(1860) Elmer Sperry	
13	T	(1890) Georg Feigl (1893) Kurt Werner Friedrich Reidemeister (1932) John Griggs Thomson	
14	F	(1687) Robert Simson (1801) Joseph Antoine Ferdinand Plateau (1868) Alessandro Padoa	
15	S	(1608) Evangelista Torricelli (1735) Jesse Ramsden (1776) Peter Barlow (1931) Eléna Wexler-Kreindler	RM165
16	S	(1879) Philip Edward Bertrand Jourdain	
42	17	M	(1759) Jacob (II) Bernoulli (1888) Paul Isaac Bernays
18	T	(1945) Margaret Dusa Waddington Mcduff	RM093 RM249
19	W	(1903) Jean Frédéric Auguste Delsarte (1910) Subrahmanyan Chandrasekhar	RM153
20	T	(1632) Sir Christopher Wren (1863) William Henry Young (1865) Aleksandr Petrovich Kotelnikov	RM105
21	F	(1677) Nicolaus (I) Bernoulli (1823) Enrico Betti (1855) Giovan Battista Guccia (1893) William Leonard Ferrar (1914) Martin Gardner	RM093 RM150 RM129 RM137
22	S	(1587) Joachim Jungius (1895) Rolf Herman Nevanlinna (1907) Sarvadaman Chowla	
23	S	(1865) Piers Bohl	
43	24	M	(1804) Wilhelm Eduard Weber (1873) Edmund Taylor Whittaker
25	T	(1811) Évariste Galois	RM069
26	W	(1849) Ferdinand Georg Frobenius (1857) Charles Max Mason (1911) Shiing-Shen Chern	
27	T	(1678) Pierre Remond de Montmort (1856) Ernest William Hobson	
28	F	(1804) Pierre François Verhulst	
29	S	(1925) Klaus Roth	
30	S	(1906) Andrej Nikolaevich Tichonov (1946) William Paul Thurston	RM237
44	31	M	(1711) Laura Maria Caterina Bassi (1815) Karl Theodor Wilhelm Weierstrass (1935) Ronald Lewis Graham



Putnam 2007, B4

Let n be a positive integer. Find the number of pairs P, Q of polynomials with real coefficients such that

$$(P(X))^2 + (Q(X))^2 = X^{2n} + 1$$
and $\deg P > \deg Q$.

Why “ π ” is inferior to “e”

‘e’ is the most commonly picked vowel in Wheel of Fortune.

Why “e” is inferior to “ π ”

π is the bigger piece of pie.

Why Astronomy is better than sex

The telescope isn't going to make you pay child support for the next eighteen years.

The pursuit of science has often been compared to the scaling of mountains, high and not so high. But who amongst us can hope, even in imagination, to scale the Everest and reach its summit when the sky is blue and the air is still, and in the stillness of the air survey the entire Himalayan range in the dazzling white of the snow stretching to infinity? None of us can hope for a comparable vision of nature and of the universe around us. But there is nothing mean or lowly in standing in the valley below and awaiting the sun to rise over Kinchinjunga.

Subrahmanyan Chandrasekhar

I think that without a doubt no one has ever tasted the sweetness of mathematical proofs, even if only brushing it with the lips, without then trying with all his might to get drunk on it to the point of satiety, although rejected by the contrasting multitude of extreme difficulties, which go with mathematics, as from dense blows; just as innumerable crowds of bees wounding him in competition with the stings can hardly ward off a bear while eating, when he has just tasted the sweetness of honey hidden in a tree.

Bonaventura Cavalieri

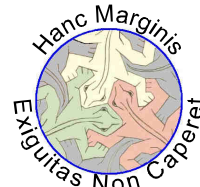
I doubt that anyone will ever be able to adequately celebrate the properties of the number 7, because they go beyond the expressible... So much august is the dignity that naturally belongs to the number 7, that it has a special and unique relationship that distinguishes it from all the other numbers: some of them generate without being generated, others are generated but do not generate, others do both, generate and are generated: the 7 alone does not belong to any of these categories. [in practice, 7 is the only number between 1 and 10 that has no divisors or multiples between 1 and 10]

Filone Di Alessandria

Juggling is sometimes called the art of controlling patterns, controlling patterns in time and space.

Ronald Lewis Graham

1	T	(1535) Giambattista della Porta	RM226	
2	W	(1815) George Boole (1826) Henry John Stephen Smith	RM094	
3	T	(1867) Martin Wilhelm Kutta (1878) Arthur Byron Coble (1896) Raymond Louis Wilder (1906) Carl Benjamin Boyer		
4	F	(1744) Johann (III) Bernoulli (1865) Pierre Simon Girard	RM093	
5	S	(1848) James Whitbread Lee Glaisher (1930) John Frank Adams		
6	S	(1906) Emma Markovna Trotskaia Lehmer	RM215	
45	7	M	(1567) Clara Immerwahr (1660) Thomas Fantet de Lagny (1799) Karl Heinrich Graffe (1878) Lise Meitner (1898) Raphael Salem	RM182 RM238
8	T	(1656) Edmond Halley (1781) Giovanni Antonio Amedeo Plana (1846) Eugenio Bertini (1848) Friedrich Ludwig Gottlob Frege (1854) Johannes Robert Rydberg (1869) Felix Hausdorff	RM190 RM154 RM274 RM178	
9	W	(1847) Carlo Alberto Castigliano (1885) Theodor Franz Eduard Kaluza (1885) Hermann Klaus Hugo Weyl (1906) Jaroslav Borisovich Lopatynsky (1913) Hedwig Eva Maria Kiesler (Hedy Lamarr) (1922) Imre Lakatos	RM202 RM082 RM144	
10	T	(1829) Helwin Bruno Christoffel		
11	F	(1904) John Henry Constantine Whitehead		
12	S	(1825) Michail Egorovich Vashchenko-Zakharchenko (1842) John William Strutt Lord Rayleigh (1927) Yutaka Taniyama		
13	S	(1876) Ernest Julius Wilkzynsky (1878) Max Wilhelm Dehn		
46	14	M	(1845) Ulisse Dini (1919) Paulette Libermann (1975) Martin Hairer	RM189
15	T	(1688) Louis Bertrand Castel (1793) Michel Chasles (1794) Franz Adolph Taurinus		
16	W	(1835) Eugenio Beltrami	RM262	
17	T	(1597) Henry Gellibrand (1717) Jean-Baptiste Le Rond D'Alembert (1790) August Ferdinand Möbius	RM166 RM118	
18	F	(1872) Giovanni Enrico Eugenio Vacca (1927) Jon Leslie Britton		
19	S	(1894) Heinz Hopf (1900) Michail Alekseevich Lavrentev (1901) Nina Karlovna Bari	RM214	
20	S	(1889) Edwin Powell Hubble (1924) Benoît Mandelbrot (1963) William Timothy Gowers		
47	21	M	(1867) Dimitri Sintsov	
22	T	(1803) Giusto Bellavitis (1840) Émile Michel Hyacinthe Lemoine		
23	W	(1616) John Wallis (1820) Issac Todhunter (1917) Elizabeth Leonard Scott	RM070 RM106	
24	T	(1549) Duncan Maclaren Young Sommerville (1909) Gerhard Gentzen		
25	F	(1841) Fredrich Wilhelm Karl Ernst Schröder (1873) Claude Louis Mathieu (1943) Evelyn Merle Roden Nelson		
26	S	(1894) Norbert Wiener (1946) Enrico Bombieri	RM172	
27	S	(1867) Arthur Lee Dixon		
48	28	M	(1898) John Wishart	
29	T	(1803) Christian Andreas Doppler (1849) Sir Horace Lamb (1879) Nikolay Mitrofanovich Krylov	RM250	
30	W	(1549) Sir Henry Savile (1969) Matilde Marcolli	RM142	



Putnam 2007, B5

Let k be a positive integer. Prove that there exist polynomials $P_0(n), P_1(n), \dots, P_{k-1}(n)$ (which may depend on k) such that for any integer n ,

$$\left\lfloor \frac{n}{k} \right\rfloor^k = P_0(n) + P_1(n) \left\lfloor \frac{n}{k} \right\rfloor + \dots + P_{k-1}(n) \left\lfloor \frac{n}{k} \right\rfloor^{k-1}$$

($\lfloor a \rfloor$ means the largest integer $\leq a$.)

Why “ π ” is inferior to “ e ”

π inferiority statements are far more concise.

Why “ e ” is inferior to “ π ”

Explaining e inferiority requires a more convoluted and precise sentence, allowing you to show your knowledge of unusual words.

Why Astronomy is better than sex

It's guaranteed to get at least a little something in view.

[A number] agrees to be taken from a greater number of itself, but to attempt to take it away from a smaller number of itself is ridiculous. Yet this is attempted by the algebrists who speak of a number smaller than nothing; or to multiply a negative number by a negative number and thus produce a positive number; or of a number that is imaginary ... It is all jargon, from which common sense withdraws; but having adopted it once, as is the case with many other fictions, it finds its staunchest supporters among those who like to accept things on trust and hate the color of serious thought.

William Frend

Medicine makes people sick, mathematics makes them sad and theology makes them sinful.

Martin Luther

To state a theorem and then to show examples of it is literally to teach backwards.

E. Kim Nebeuts

There still remain three studies suitable for free man. Arithmetic is one of them.

Plato

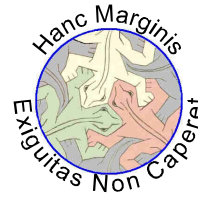
[Wrote to La Condamine, after he delivered equator's measure] "Vous avez trouve par de long ennuis ce que Newton trouva sans sortir de chez lui" – With huge effort you have discovered what Newton calculated without leaving home.

Voltaire

Mathematics has beauties of its own – a symmetry and proportion in its results, a lack of superfluity, an exact adaptation of means to ends, which is exceedingly remarkable and to be found only in the works of the greatest beauty. When this subject is properly... presented, the mental emotion should be that of enjoyment of beauty, not that of repulsion from the ugly and the unpleasant.

Jacob William Albert Young

1	T	(1792) Nikolay Yvanovich Lobachevsky (1847) Christine Ladd-Franklin	RM083	
2	F	(1831) Paul David Gustav du Bois-Reymond (1869) Dimitri Fedorovich Egorov (1901) George Frederick James Temple	RM214	
3	S	(1903) Sidney Goldstein (1924) John Backus		
4	S	(1795) Thomas Carlyle		
49	5	M	(1868) Arnold Johannes Wilhelm Sommerfeld (1901) Werner Karl Heisenberg (1907) Giuseppe Occhialini	RM275 RM155 RM122
	6	T	(1682) Giulio Carlo Fagnano dei Toschi	
	7	W	(1823) Leopold Kronecker (1830) Antonio Luigi Gaudenzio Giuseppe Cremona (1924) Mary Ellen Rudin	RM239 RM150
	8	T	(1508) Regnier Gemma Frisius (1865) Jaques Salomon Hadamard (1919) Julia Bowman Robinson	RM263 RM227
	9	F	(1883) Nikolai Nikolaievich Luzin (1906) Grace Brewster Murray Hopper (1917) Sergei Vasilovich Fomin	RM214
	10	S	(1804) Karl Gustav Jacob Jacobi (1815) Augusta Ada King Countess Of Lovelace	RM251 RM059
	11	S	(1882) Max Born	RM155
50	12	M	(1832) Peter Ludwig Mejdell Sylow (1913) Emma Castelnuovo	RM191
	13	T	(1724) Franz Ulrich Theodosius Aepinus (1887) George Pólya	RM131
	14	W	(1546) Tycho Brahe	
	15	T	(1802) János Bolyai (1923) Freeman John Dyson	RM083
	16	F	(1804) Wiktor Yakovievich Bunyakowsky	
	17	S	(1706) Gabrielle Émilie Le Tonnelier de Breteuil du Châtelet (1835) Felice Casorati (1842) Marius Sophus Lie (1900) Dame Mary Lucy Cartwright	
	18	S	(1856) Joseph John Thomson (1917) Roger Lyndon (1942) Lenore Blum	RM161
51	19	M	(1783) Charles Julien Brianchon (1854) Marcel Louis Brillouin (1887) Charles Galton Darwin	RM138
	20	T	(1494) Oronce Fine (1648) Tommaso Ceva (1875) Francesco Paolo Cantelli	RM203
	21	W	(1878) Jan Łukasiewicz (1921) Edith Hirsch Luchins (1932) John Robert Ringrose	
	22	T	(1824) Francesco Brioschi (1859) Otto Ludwig Hölder (1877) Tommaso Boggio (1887) Srinivasa Aiyangar Ramanujan	RM150
	23	F	(1872) Georgii Yurii Pfeiffer	
	24	S	(1822) Charles Hermite (1868) Emmanuel Lasker	RM095 RM167
	25	S	(1642) Isaac Newton (1900) Antoni Zygmund	RM071
52	26	M	(1780) Mary Fairfax Greig Somerville (1791) Charles Babbage (1937) John Horton Conway	RM059 RM119
	27	T	(1571) Johannes Kepler (1654) Jacob (Jacques) Bernoulli	RM093
	28	W	(1808) Louis Victoire Athanase Dupré (1882) Arthur Stanley Eddington (1903) John von Neumann	RM179 RM107
	29	T	(1856) Thomas Jan Stieltjes	
	30	F	(1897) Stanislaw Saks	
	31	S	(1872) Volodymyr Levitsky (1896) Carl Ludwig Siegel (1945) Leonard Adleman (1952) Vaughan Frederick Randall Jones	RM143



Putnam 2007, B6

For each positive integer n , let $f(n)$ be the number of ways to make $n!$ cents using an unordered collection of coins, each worth $k!$ cents for some k , $1 \leq k \leq n$. Prove that for some constant C , independent of n ,

$$n^{\frac{n^2}{2}-Cn} e^{-n^2/4} \leq f(n) \leq n^{\frac{n^2}{2}+Cn} e^{-n^2/4}.$$

Why “ π ” is inferior to “ e ”

Applying a simple sine function to π gives zero.

Why “ e ” is inferior to “ π ”

$$2 < e < 3 < \pi < 4.$$

Why Astronomy is better than sex

You don't have to compliment the person that gave you a view.

The original source of the word “mathematics” is the Greek verb meaning “to understand” or “to learn”. Mathematics is also essentially an art, but its primary purpose is to create rationally coherent thought structures that are therefore suitable for understanding or learning. The “medium” of mathematical art is therefore abstract symbolic thinking, while what is usually called art uses a sensory perceivable medium. The two types of art differ in this.

David Bohm

Since you are studying geometry and trigonometry, I'll give you a problem. A ship plows the ocean. You left Boston with a 200-ton load of wool on your way to Le Havre. The mainmast is broken, a hub is on the deck, the wind is blowing from the east-north-east, it's a quarter past three in the afternoon. We are in May. What is the age of the captain?

Gustave Flaubert

Geometry has two great treasures: one is the Pythagorean theorem; the other, the division of a segment according to the harmonic proportion. We can compare the former to a quantity of gold, and the latter to a precious jewel.

Johannes Kepler

I have not been able to discover the cause of those properties of gravity from phenomena, and I frame no hypotheses; for whatever is not deduced from the phenomena is to be called a hypothesis, and hypotheses, whether metaphysical or physical, whether of occult qualities or mechanical, have no place in experimental philosophy.

Isaac Newton

Mathematics is about proving the most obvious thing in the least obvious way.

George Polya

Mathematics is less related to accounting than it is to philosophy.

Leonard Adleman